



Lebanese American University  
School of Engineering  
IME Department

**MEE 403 HEAT TRANSFER**  
**First Midterm, Duration 90 min**

**Name:**

**April 16, 2013**

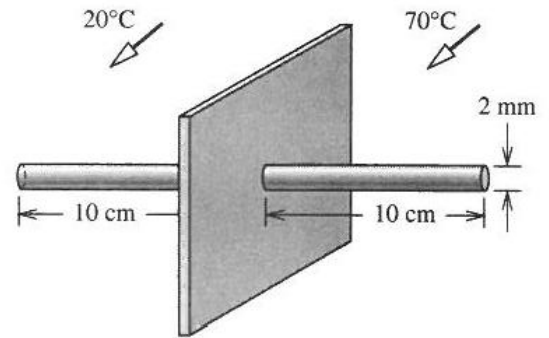
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- 1 (25 pts) A plane wall of thickness  $2L=40$  mm and thermal conductivity  $k=5$  W/m.K experiences uniform volumetric heat generation at a rate  $\dot{q}$ , while convection heat transfer occurs at both of its surface ( $x=-L, +L$ ), each of which is exposed to a fluid of temperature  $T_\infty=20^\circ\text{C}$ . Under steady-state conditions, the temperature distribution in the wall is of the form  $T(x)=a+bx+cx^2$ , where  $a= 82^\circ\text{C}$ ,  $b=-210^\circ\text{C/m}$ ,  $c=-2\times 10^{-4}^\circ\text{C/m}^2$ , and  $x$  is in meters. The origin of the  $x$ -coordinate is at the midplane of the wall.
- Sketch the temperature distribution and identify significant physical features
  - What is the volumetric rate of heat generation  $\dot{q}$  in the wall?
  - Determine the surface heat fluxes,  $q_x''(-L)$  and  $q_x''(+L)$ . How are these fluxes related to the heat generation rate?
  - What are the convection coefficients for the surfaces at  $x=-L$  and  $x=+L$ ?
  - If the source of the heat generation is suddenly deactivated ( $\dot{q} = 0$ ), what is the rate of change of energy stored in the wall at this instant?

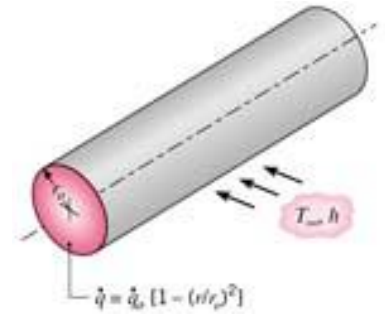


- 2 (25 pts) Two air flows are separated by a 2 mm-thick plastic wall. A 20.2 cm-long, 1 cm-diameter aluminum rod transfers heat from one flow to the other as shown. The hot air flow is at  $70^{\circ}\text{C}$ , and the convective heat transfer coefficient to the rod is  $48 \text{ W/m}^2 \text{ K}$ ; the cold air flow is at  $20^{\circ}\text{C}$  and is at a lower velocity, giving a heat transfer coefficient of only  $24 \text{ W/m}^2 \text{ K}$ . Determine the rate of heat transfer and the temperature of the midsection of the rod. Take  $k=190 \text{ W/m K}$  for the aluminum.





- 3 (25 pts) Radioactive wastes are packed in a long, thin-walled cylindrical container, the wastes generate thermal energy nonuniformly according to the relation  $\dot{q}(r) = \dot{q}_o \left[ 1 - (r/r_o)^2 \right]$ , where  $\dot{q}$  is the local rate of energy generation per unit volume,  $\dot{q}_o$  is a constant, and  $r_o$  is the radius of the container. Steady-state conditions are maintained by submerging the container in a liquid that is at  $T_\infty$  and provides a uniform convection coefficient  $h$ . Obtain an expression for the total rate at which energy is generated in a unit length of the container. Use this result to obtain an expression for the temperature  $T_s$  of the container wall.





- 4 (25 pts) A 60 cm long, 3 cm- diameter AISI 1010 steel rod  $k=64 \text{ W/m K}$  is welded to a furnace wall and passes thru 20 cm of insulation before emerging into the surrounding air. The furnace wall is at  $300^\circ\text{C}$ , and the air temperature is  $20^\circ\text{C}$ . Estimate the temperature of the bar tip if the heat transfer coefficient between the rod and the air is taken to be  $13 \text{ w/m}^2\text{K}$

